

# Phenotypic switching as a mechanism to circumvent fitness valleys

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CHEMISTRY OF BACTERIA



**IChF**

# Acknowledgments



**Andrew Tadrowski**



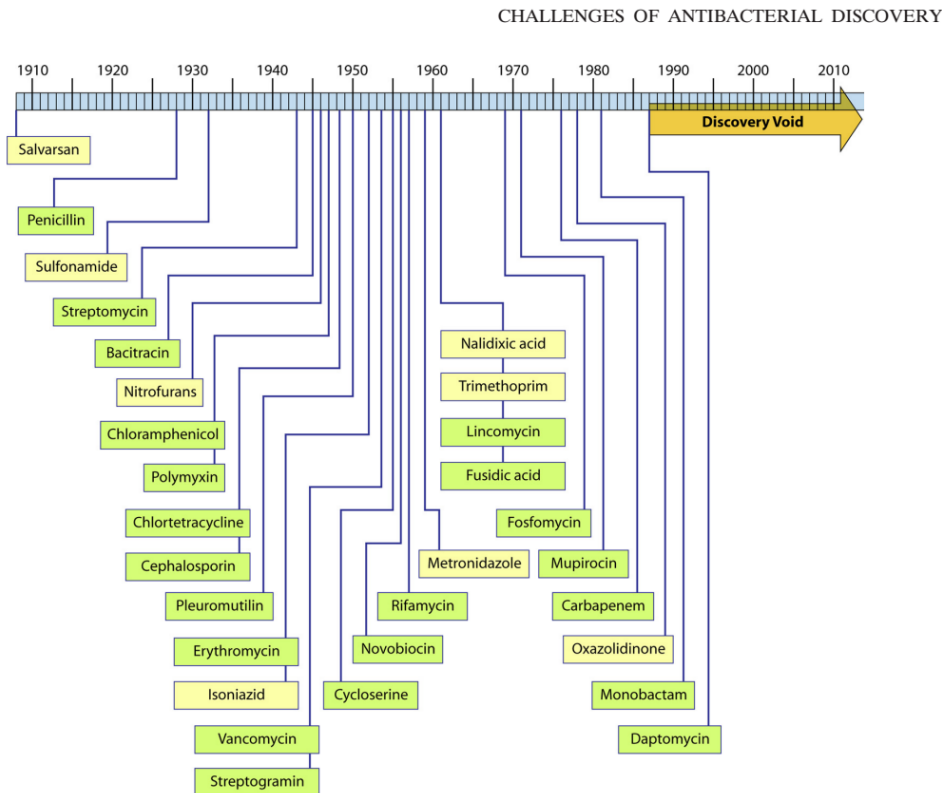
**Martin Evans**



# Motivation: bacterial infections

Responsible for 1.3M deaths/year worldwide. May increase to 10M/y by 2050.

## Resistance to antibiotics is a concern



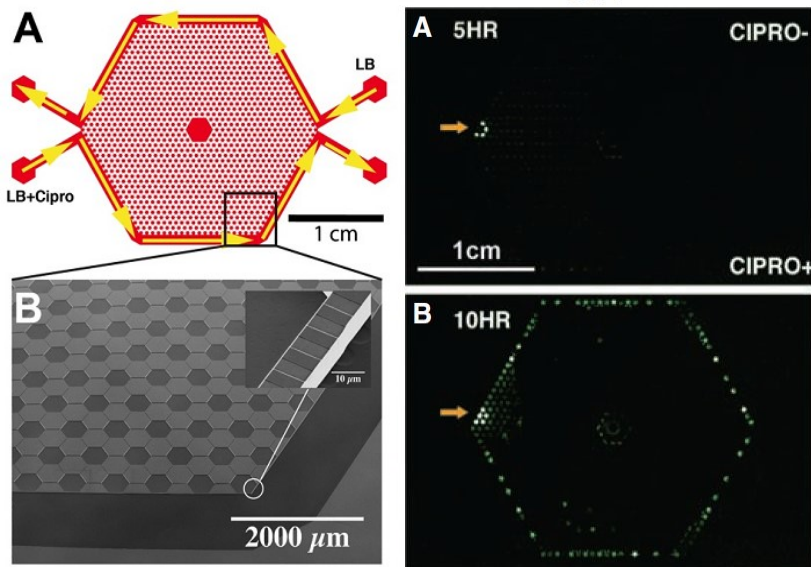
Better prevention, diagnostics, and treatment required

What we do:  
**quantitative understanding of bacterial infections and antibiotic resistance**

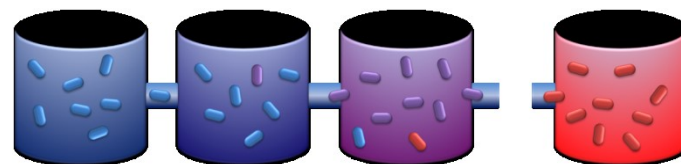
- modelling
- experiments

# Rapid evolution of resistance in drug gradients – insight from modelling

Q. Zhang, et al., *Science* **333**, 1764-1767 (2011)



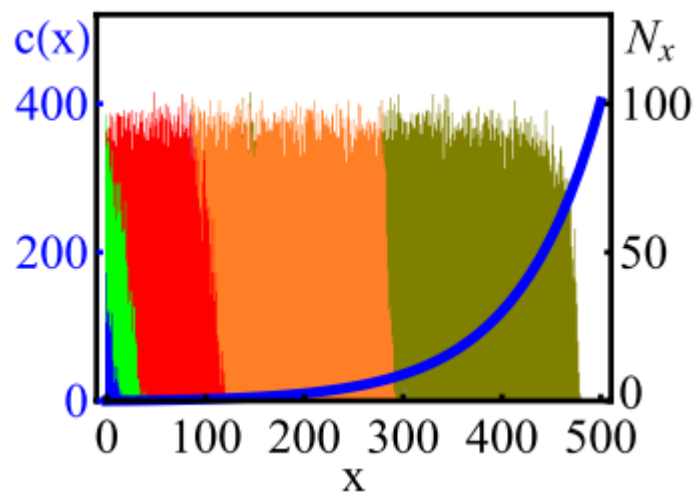
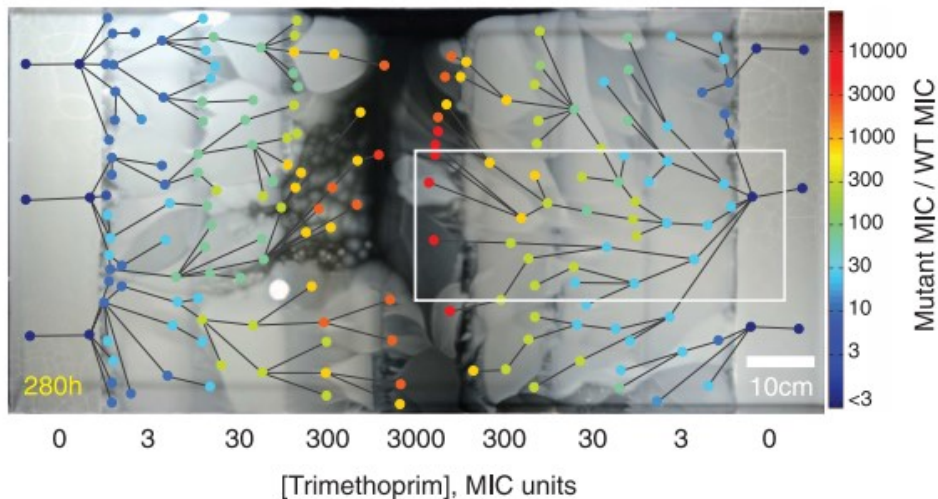
P. Greulich, B. Waclaw, R. Allen, *Phys. Rev. Lett.* **109**, 088101 (2012)



low drug concentration

high drug concentration

M. Baym, et al, *Science* **353**, 1147 (2016)



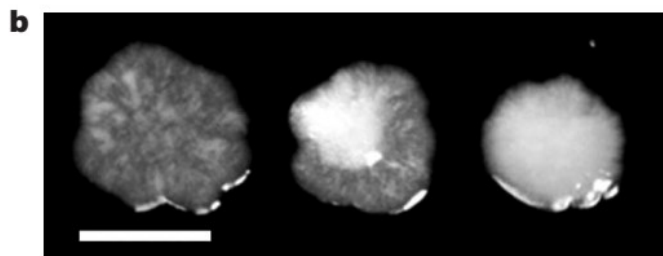
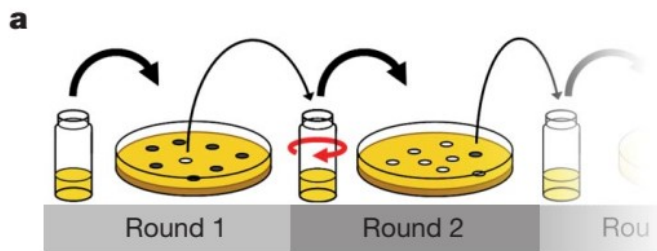
# Phenotype switching

Phenotypic plasticity: capacity to change phenotype in response to environmental changes – without change to its genotype. All organisms do it.

Stochastic phenotype switching (SPS) occurs without any sensing mechanism - this is what we're interested in.

A 'bet-hedging' strategy: beneficial for when environmental changes are frequent and unpredictable.

SPS is commonly observed in bacteria



experimental

- H. J. E. Beaumont, et al., *Nature* **462**, 90 (2009).
- Y. Ito, et al., *Mol Syst Biol* **5**, 264 (2009).
- A. Solopova, et al., *PNAS* **111**, 7427 (2014).
- M. Arnoldini, et al., *PLoS Biol* **12**, e1001928 (2014).
- H. Hasman, et al., *Journal of Bacteriology* **182**, 1089 (2000).

theory

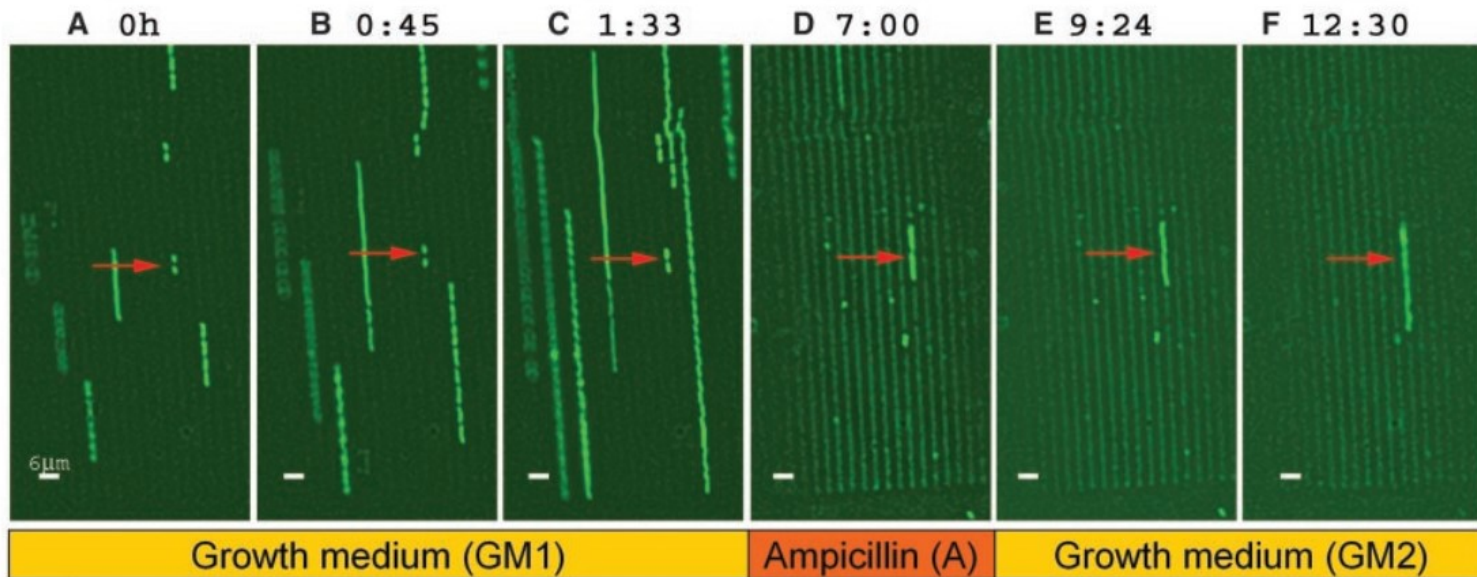
- E. Kussell and S. Leibler, *Science* **309**, 2075 (2005).
- P. Ashcroft, et al., *J. R. Soc. Interface* **11**, 20140663 (2014).
- A. Taitelbaum, et al., *Phys. Rev. Lett.* **125**, 048105 (2020).

theory+experiment

- N. Q. Balaban, et al., *Science* **305**, 1622 (2004).
- M. Acar, et al., *Nature Genetics* **40**, 471 (2008).

# SPS example – bacterial persistence

*Escherichia coli* can switch between normal and persister states. Persister cells grow at a slower rate than the normal cells but are resistant to antibiotics

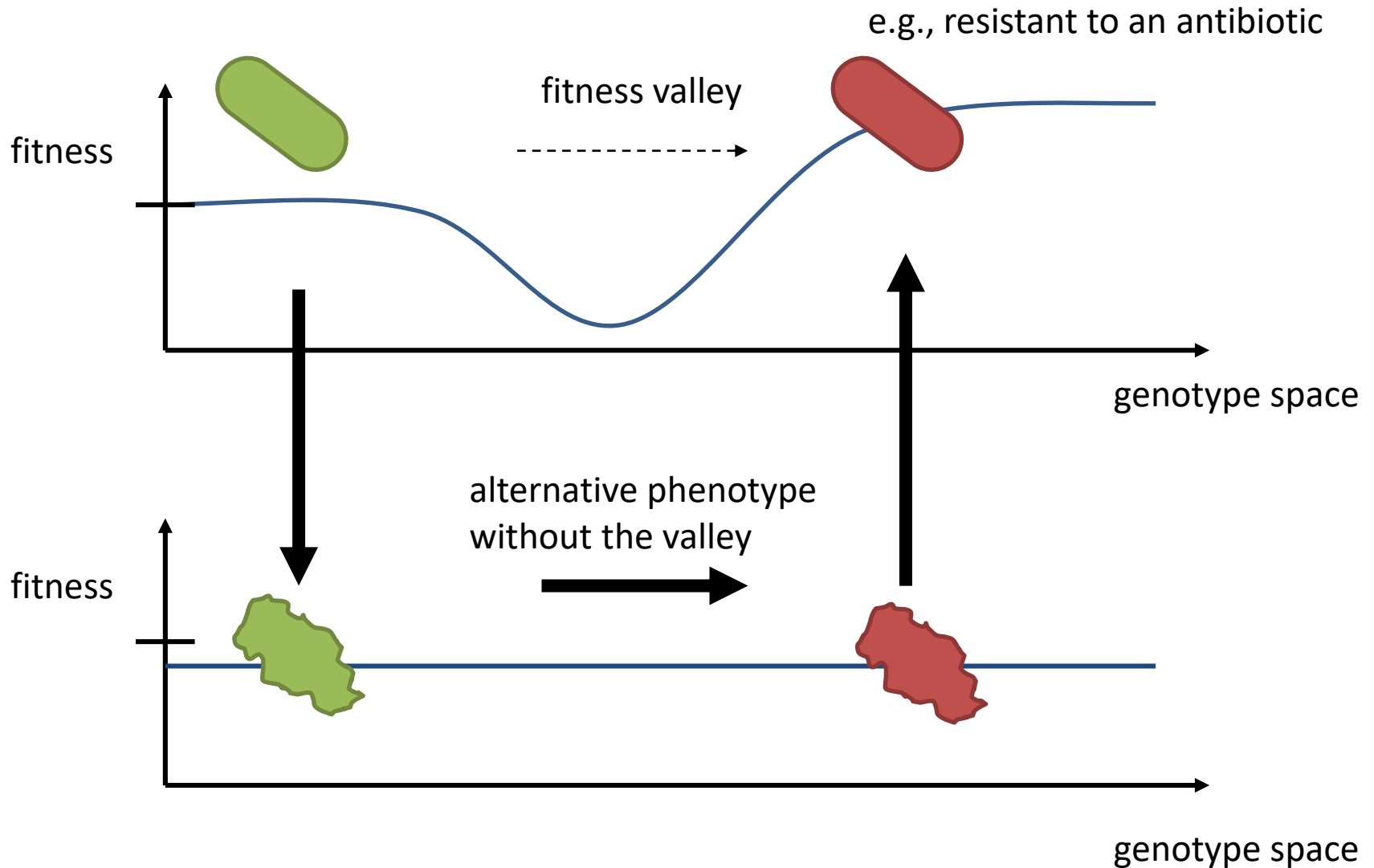


Balaban et al. Science 2004

Could persistence speed up evolution by providing a “safe haven” for bacteria to try out different mutations?

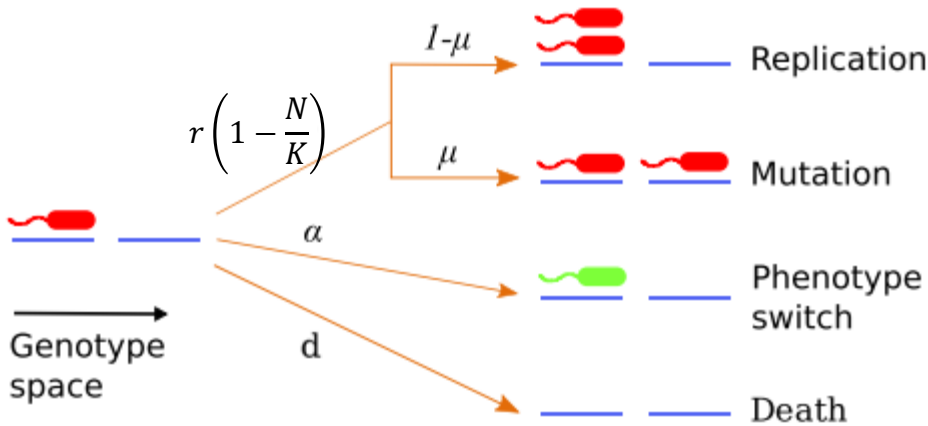
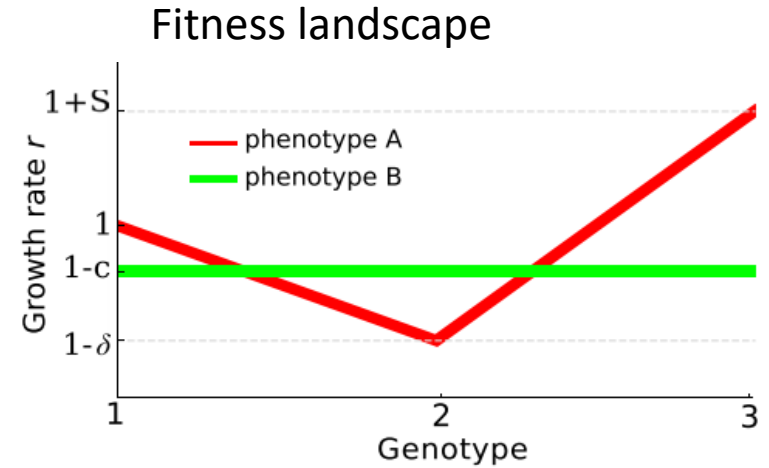
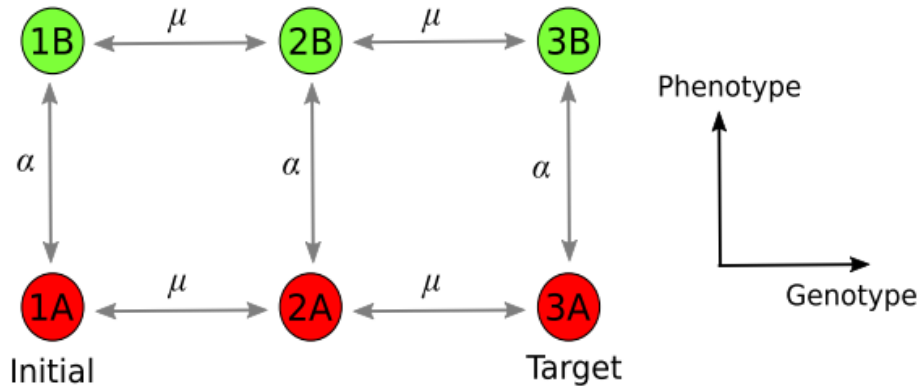
**More generally: Could phenotype switching help to avoid fitness valleys?**

# A 1-slide summary of this talk:



# A simple model

3 genotypes x 2 phenotypic states



Important parameters:

$\alpha$  – switching rate

$\delta$  – valley depth

$\mu$  – mutation probability

$K$  – carrying capacity



# More formally...

State:  $C = (n_{1A}, n_{2A}, n_{3A}, n_{1B}, n_{2B}, n_{3B})$ ,  $n_i = 0, \dots, K$

Master equation

$$\frac{\partial P(C, t)}{\partial t} = \sum_{C' \neq C} (P(C', t)w(C' \rightarrow C) - P(C, t)w(C \rightarrow C'))$$

$w(C \rightarrow C')$  are transition rates, for example

$$w(\{n_{1A}, \dots, n_{1B}, \dots\} \rightarrow \{n_{1A} - 1, \dots, n_{1B} + 1, \dots\}) = \alpha$$

$$w(\{n_{1A}, \dots\} \rightarrow \{n_{1A} + 1, \dots\}) = (1 - \mu)r_{1A} \left(1 - \frac{N}{K}\right)$$

phenotype  
switching

growth

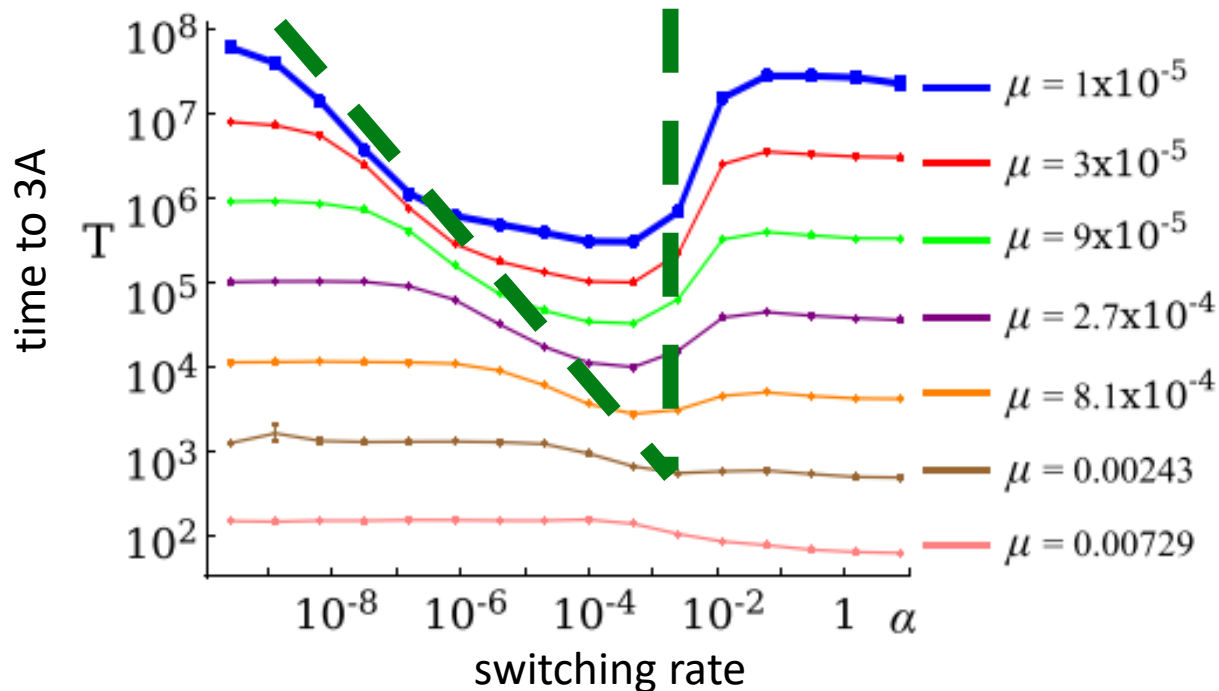
etc.

We simulate the model on a computer using different techniques depending on which observable we are interested in (exact kinetic MC, tau-leaping)

Approximate analytic solutions available in some regimes (won't talk much about it)

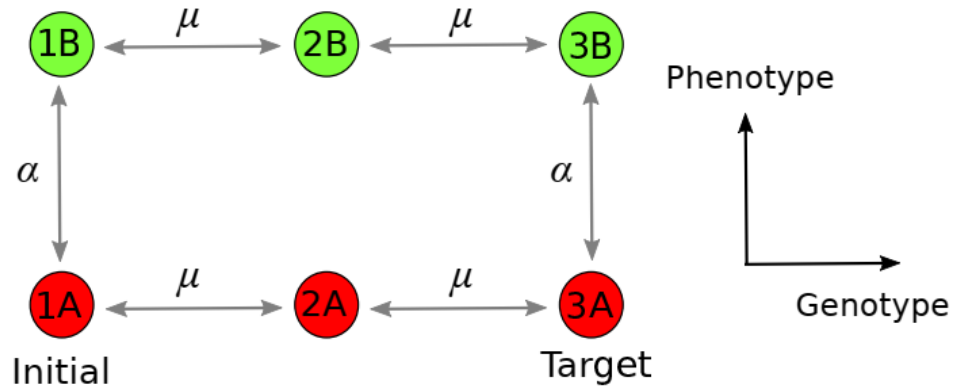
# Results for no fitness cost for the 2<sup>nd</sup> phenotype ( $c = 0$ )

We measure the time to obtain a single organism of the best-adapted phenotype 3A  
Small system ( $K=100$ ), low mutation ( $\mu = 10^{-5} \dots 10^{-2}$ ,  $K\mu < 1$ ),  $\delta = 0.4$ ,  $d = 0.1$

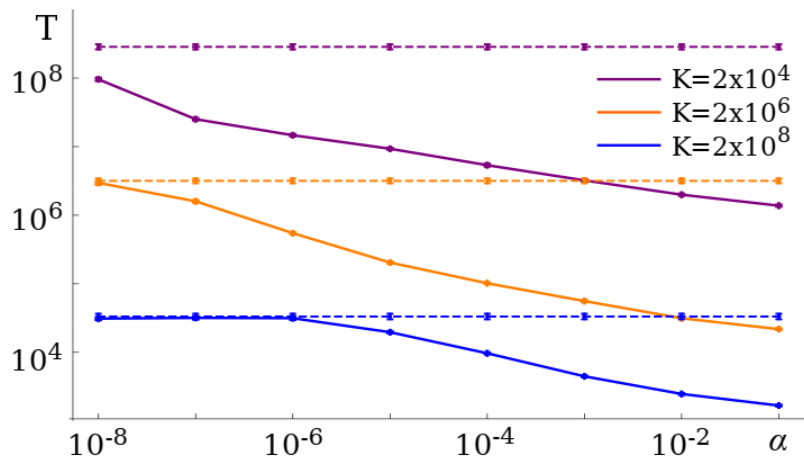


Optimal switching rate exists for a broad range of mutation rates

# Time to adaptation decreases monotonically in the absence of $2A \leftrightarrow 2B$ transition



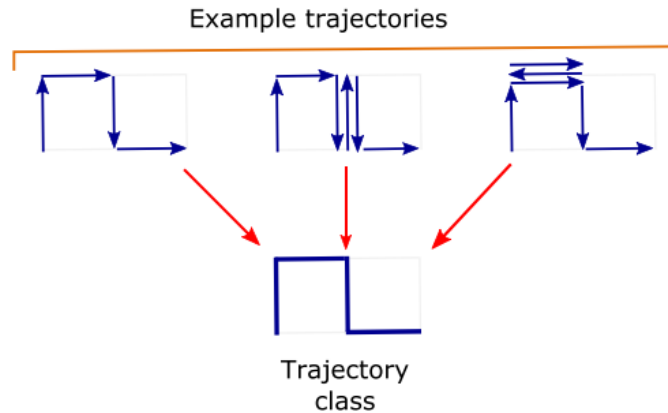
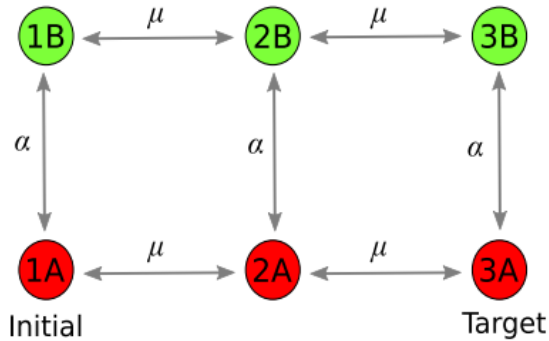
$$\mu = 10^{-6}$$



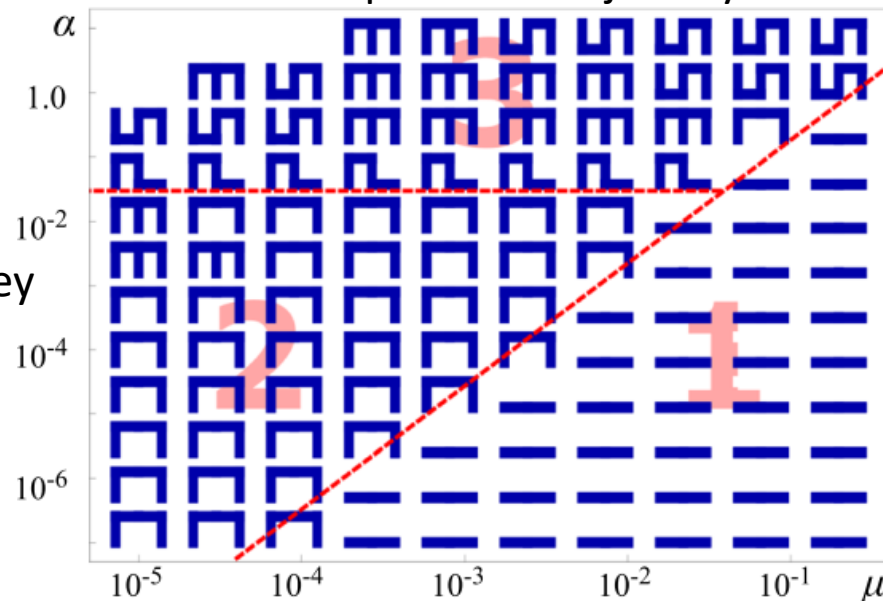
Reason:

rapid transitions  $2A \leftrightarrow 2B$   
(absent here) create an effective  
fitness valley at genotype 2

# Fastest trajectories avoid the fitness valley



Most probable trajectory:



**3** = mixed trajectories (responsible for increase in  $T$  for large  $\alpha$ )

**1** = going through the valley


**2** = going around the valley (switch from A to B)

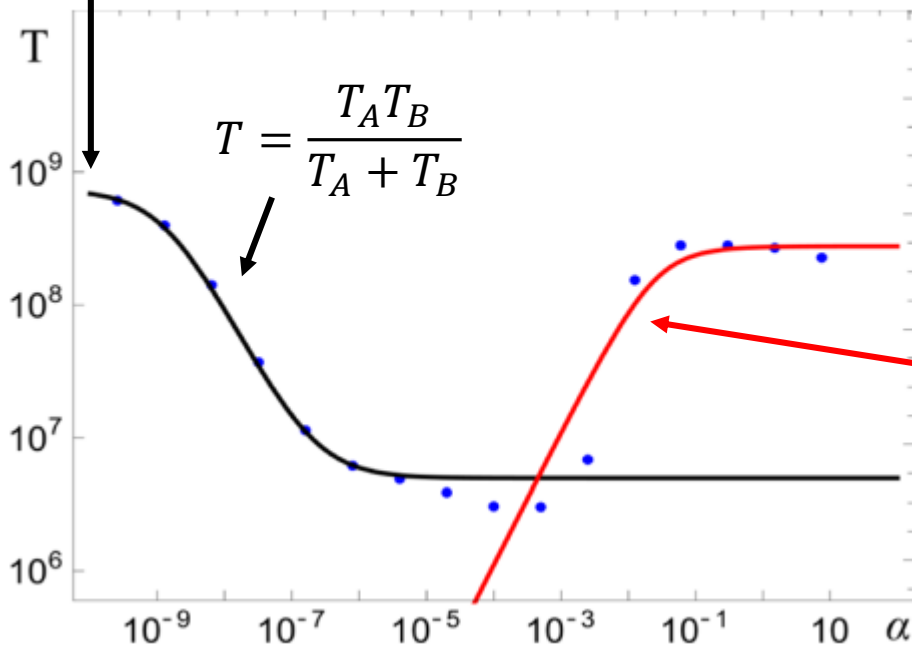
# Time to adaptation for different trajectories

$$T_A \approx \frac{1}{(1-d)K\mu^2 d(1/\delta - 1)}$$

 tunnelling through the barrier for **small  $\alpha$**

$$T_B \approx \frac{1}{\alpha} + \frac{5}{\mu d}$$

 switching to the alternate phenotype B for **intermediate  $\alpha$**



$$T = \frac{T_A T_B}{T_A + T_B}$$

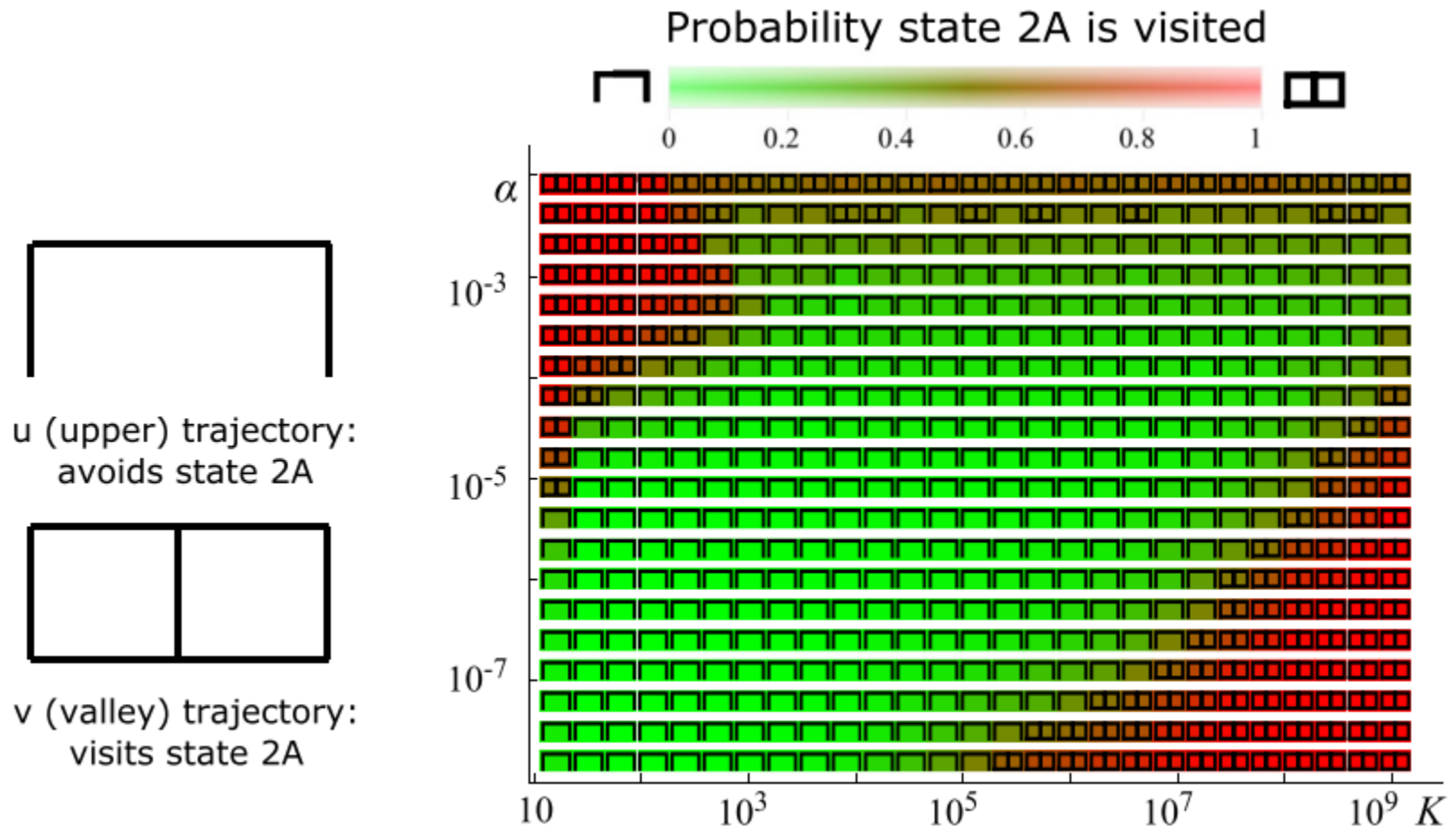


**large  $\alpha$** : tunnelling through the “effective” fitness valley made of combined 2A and 2B:

$$T_{\text{comb,ST}} \approx \frac{1}{(1-d)K\mu^2 d(1/(1-r_{2,\text{comb}}) - 1)}$$

$$\begin{aligned} r_{2,\text{comb}} &= n_{2A}r_{2A} + n_{2B}r_{2B} \\ &= \frac{(d+\alpha)(2-\delta) + \sqrt{\delta^2(\alpha+d)^2 - 4\alpha^2(\delta-1)}}{2(2\alpha+d)} \end{aligned}$$

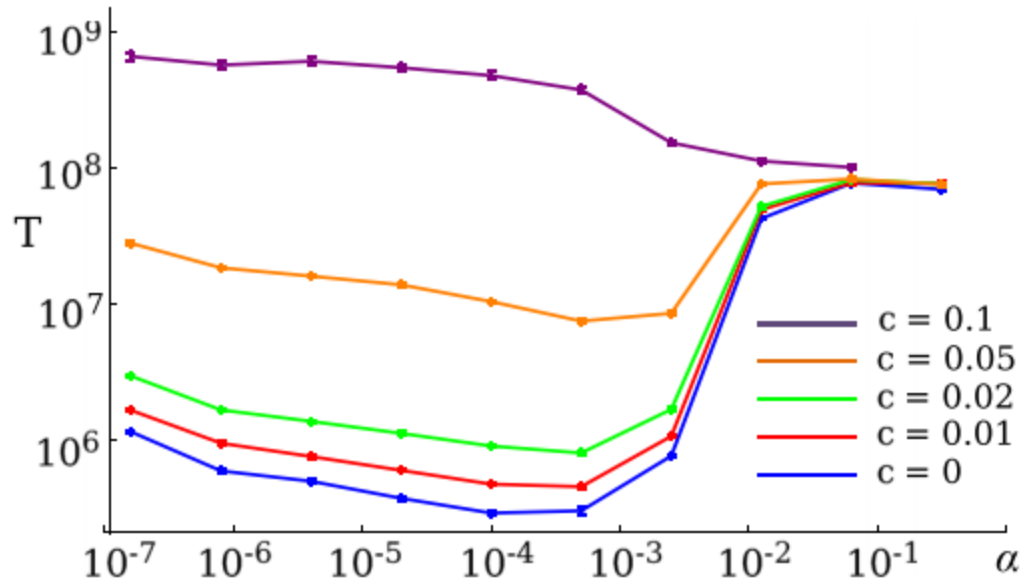
# Phenotype switching is favoured in a large region of parameter space



Here  $\mu = 10^{-6}$ ,  $\alpha \sim 10^{-3}$ ,  $K \sim 10^9$  - biologically realistic values

# Switching phenotypes remains advantageous also for fitness cost $c > 0$

$$K = 100, \delta = 0.9, d = 0.1, \mu = 10^{-5}$$

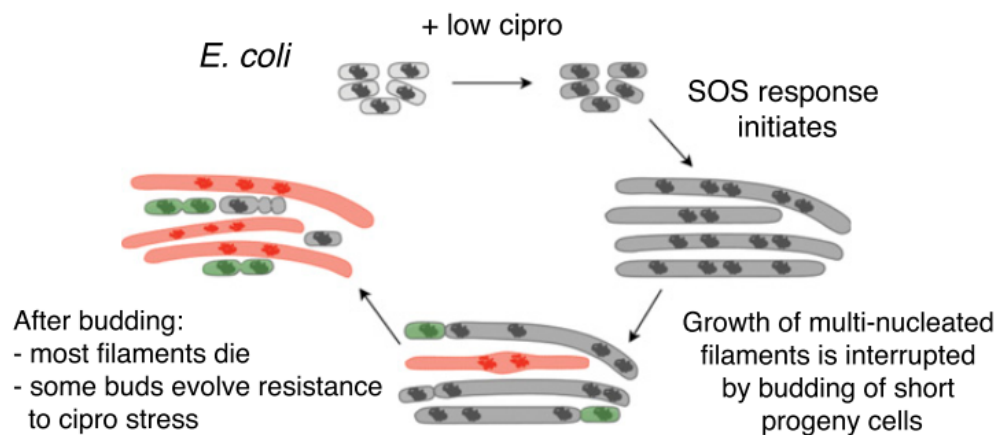


- phenotype switching still reduces time to adaptation
- no optimal switching rate for larger  $c$

# Experimental evidence?

Idealized model, not meant to reproduce any specific experiment

However: some evidence that a similar mechanism may be relevant for the antibiotic ciprofloxacin

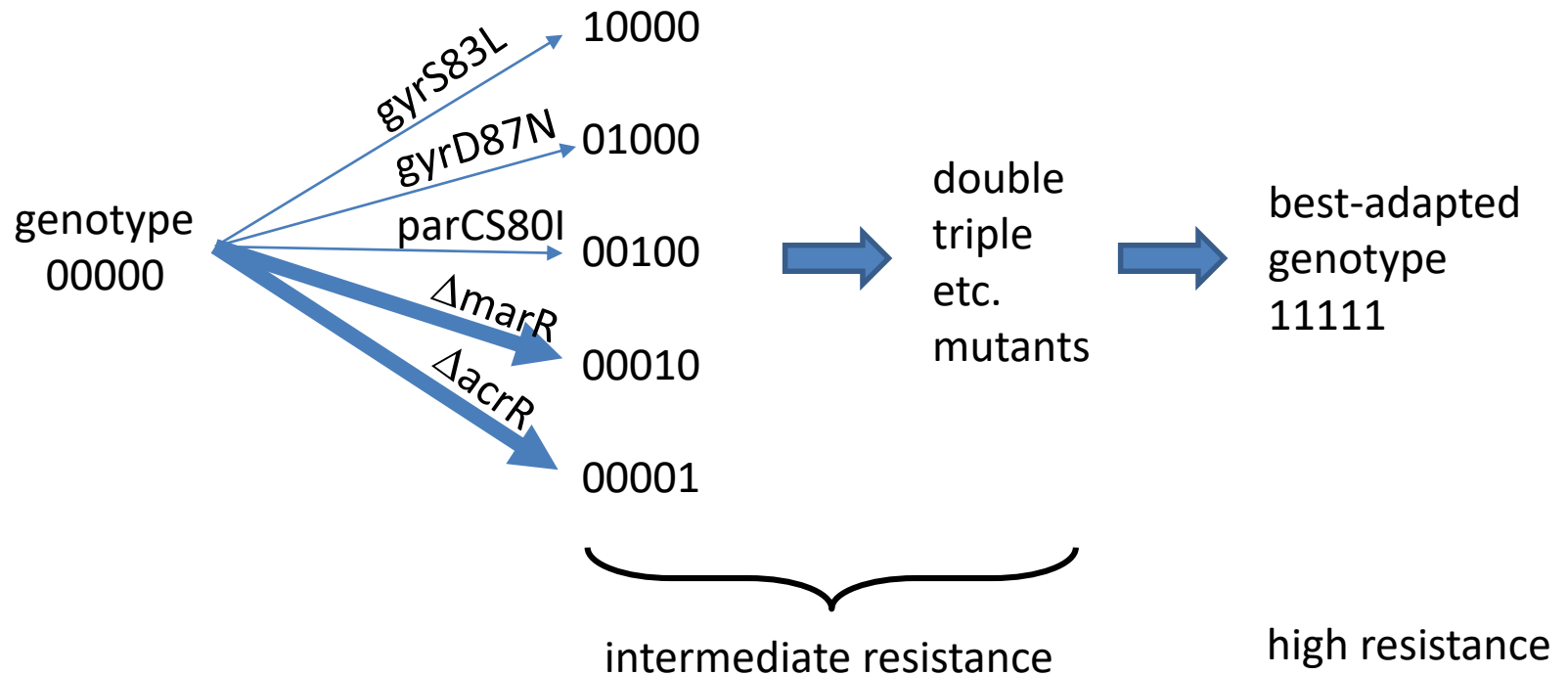


J. Bos, Q. Zhang, S. Vyawahare, E. Rogers, S. M. Rosenberg, and R. H. Austin, *Emergence of Antibiotic Resistance from Multinucleated Bacterial Filaments*, PNAS 2015.

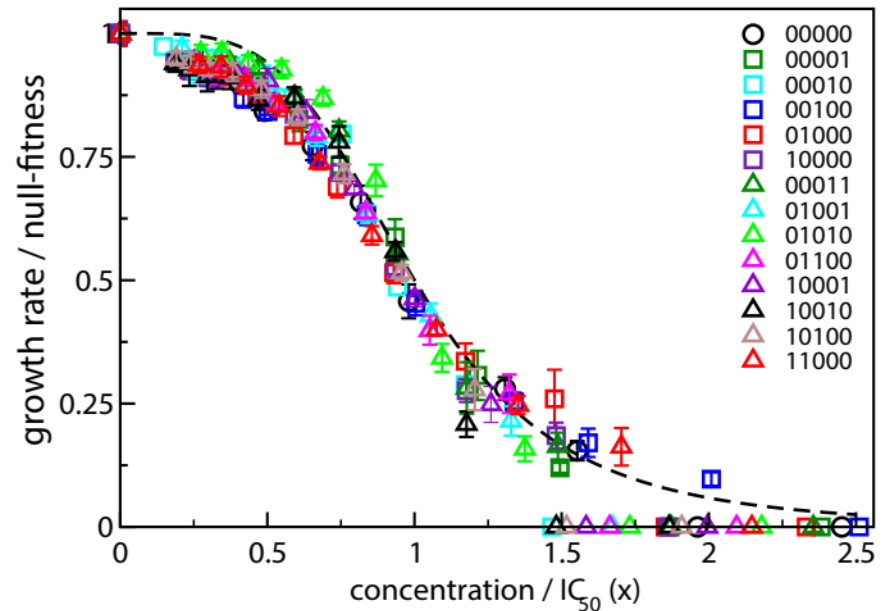
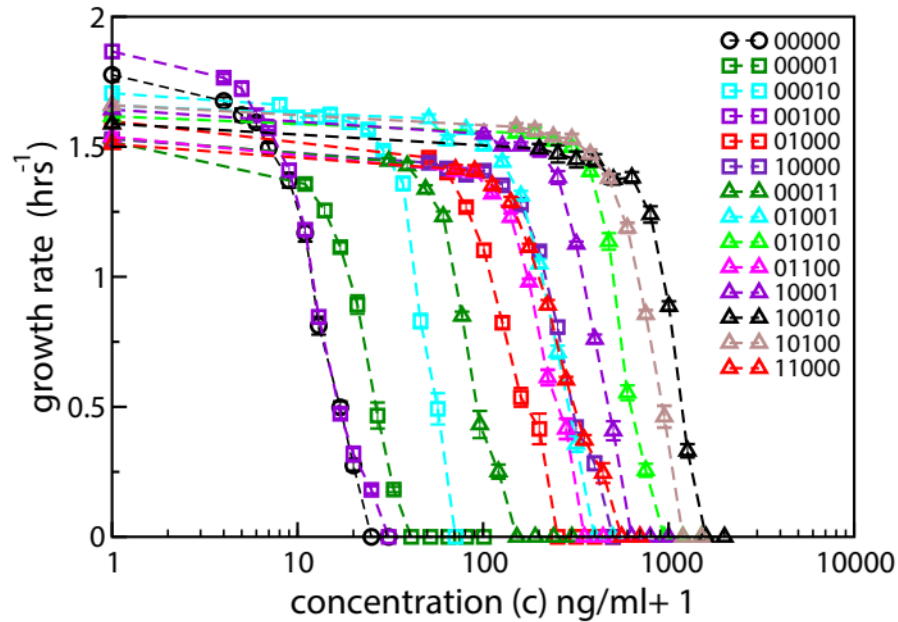


# Evolution of resistance to the antibiotic ciprofloxacin

5 specific mutations increase resistance of *E. coli* by 3 orders of magnitude  
We represent mutants by binary sequences:



# The fitness of mutants depends on antibiotic concentration

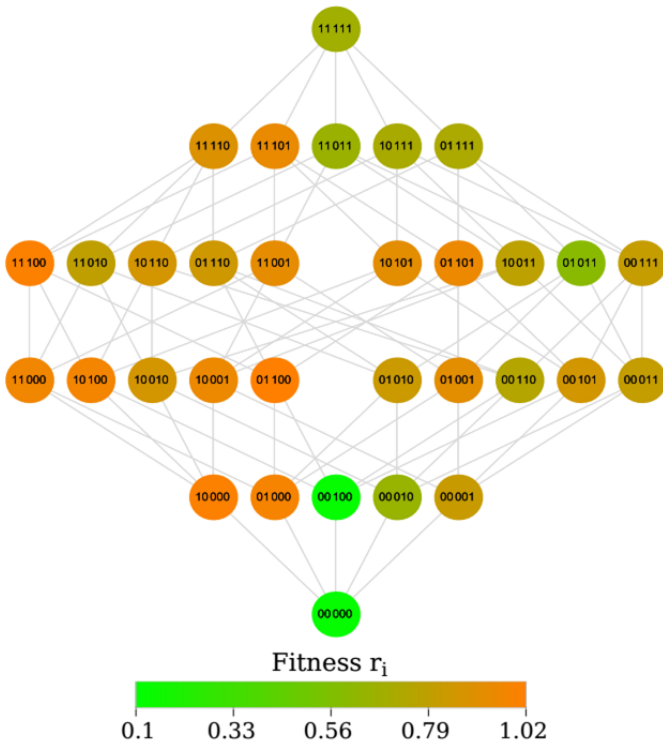


the curve

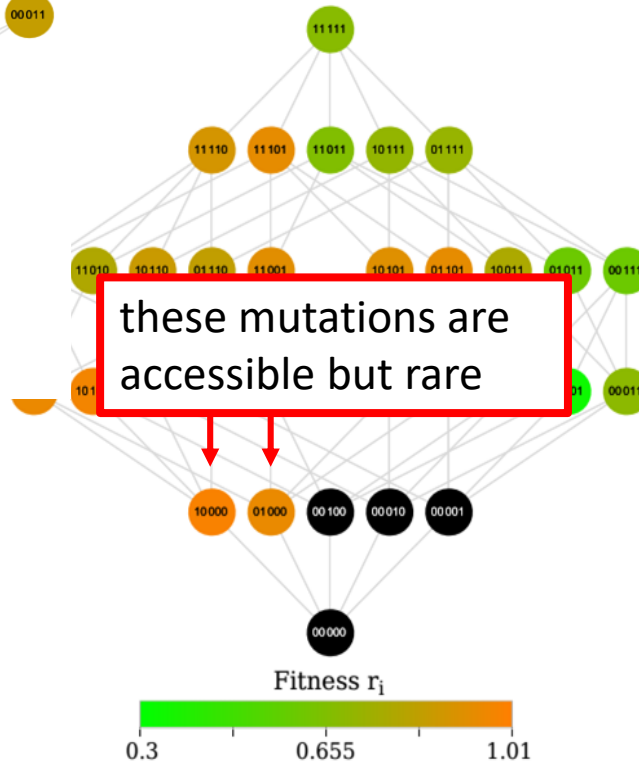
*growth rate(antibiotic conc.)*

has the same shape for all mutants

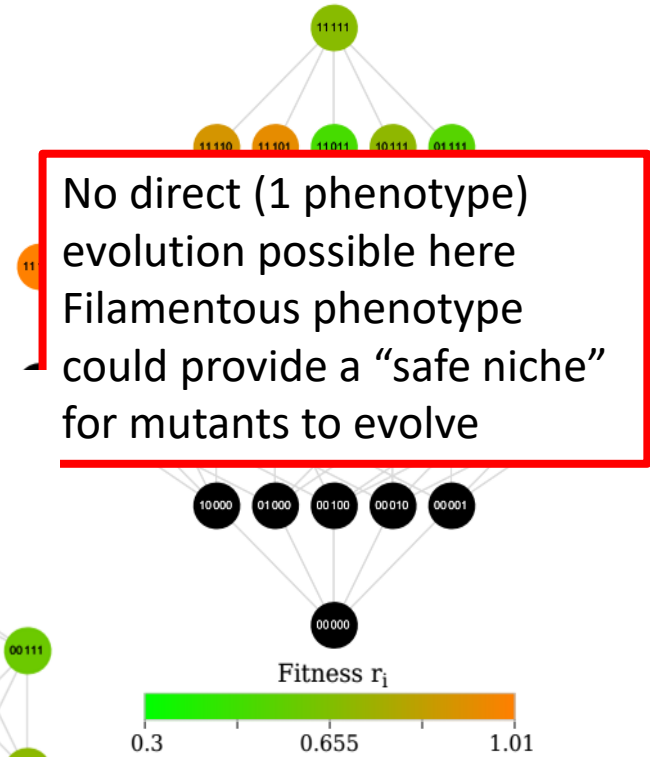
# Fitness landscapes



sub-inhibitory Cipro  
(0.9x MIC WT)



intermediate Cipro (3x MIC WT)

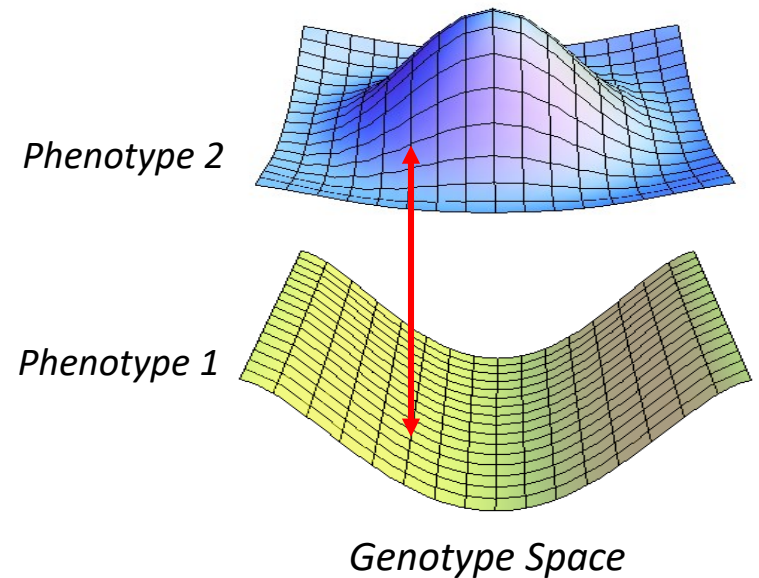


high Cipro (60x MIC WT)

= lethal genotype

# Conclusions

- stochastic phenotype switching ubiquitous in microbes
- possible roles: division of labour, bet hedging
- here: **provides a way to circumvent fitness valleys by switching to an alternate fitness landscape**
- speed gain: potentially orders of magnitude
- some evidence that it may be relevant for antimicrobial resistance evolution



Paper:

A. C. Tadrowski, M. R. Evans, and B. Waclaw, *Scientific Reports* **8**, 8941 (2018).

Also

Bacterial growth: A statistical physicist's guide

RJ Allen, B Waclaw, *Reports on Progress in Physics* **82** (1), 016601 (2018)